

On the extent of separable, locally compact, selectively (a) -spaces

Samuel G. da Silva

Universidade Federal da Bahia, Brazil

Resumo

The author has recently shown that separable, selectively (a) -spaces cannot include closed discrete subsets of size \mathfrak{c} . It follows that, assuming **CH**, separable selectively (a) -spaces have, necessarily, countable extent. However, it was also shown by the author that the weaker hypothesis “ $2^{\aleph_0} < 2^{\aleph_1}$ ” is not enough to ensure countability of the closed discrete subsets of such spaces. In this note we show that, if one adds the hypothesis of local compactness, then a specific effective (meaning, Borel) parametrized weak diamond principle implies countable extent in this context.